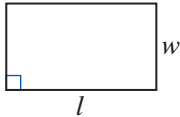
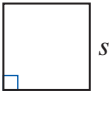
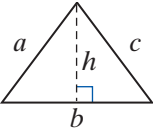
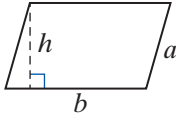
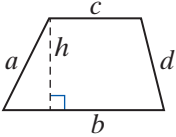
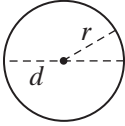


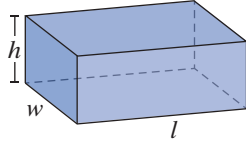
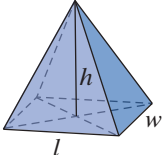
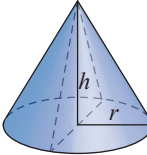
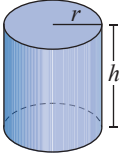
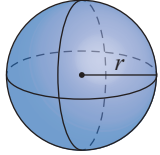
# Geometry

$P$  = Perimeter,  $A$  = Area,  $C$  = Circumference,  $V$  = Volume

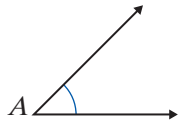
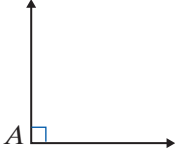
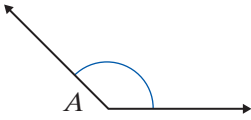
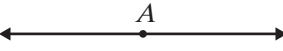
## Perimeter and Area

Rectangle	Square	Triangle	Parallelogram	Trapezoid	Circle
$P = 2l + 2w$	$P = 4s$	$P = a + b + c$	$P = 2a + 2b$	$P = a + b + c + d$	$C = 2\pi r = \pi d$
$A = lw$	$A = s^2$	$A = \frac{1}{2}bh$	$A = bh$	$A = \frac{1}{2}h(b+c)$	$A = \pi r^2$
					

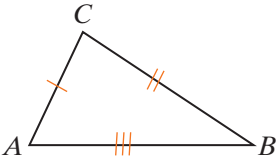
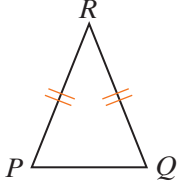
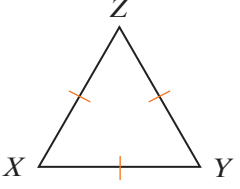
## Volume

Rectangular Solid	Rectangular Pyramid	Right Circular Cone	Right Circular Cylinder	Sphere
$V = lwh$	$V = \frac{1}{3}lwh$	$V = \frac{1}{3}\pi r^2 h$	$V = \pi r^2 h$	$V = \frac{4}{3}\pi r^3$
				

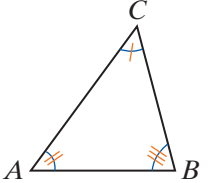
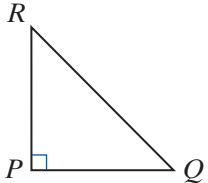
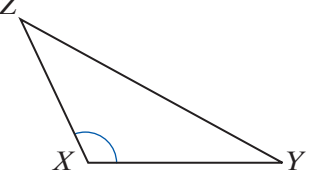
## Angles Classified by Measure

Acute	Right	Obtuse	Straight
$0^\circ < m\angle A < 90^\circ$	$m\angle A = 90^\circ$	$90^\circ < m\angle A < 180^\circ$	$m\angle A = 180^\circ$
			

## Triangles Classified by Sides

Scalene	Isosceles	Equilateral
No two sides are equal.	At least two sides are equal.	All three sides are equal.
		

## Triangles Classified by Angles

Acute	Right	Obtuse
All three angles are acute.	One angle is a right angle.	One angle is obtuse.
		

## US Customary System of Measurement

## Metric System of Measurement

### Length

12 inches (in.) = 1 foot (ft)  
 3 feet = 1 yard (yd)  
 36 inches = 1 yard  
 5280 feet = 1 mile (mi)

### Capacity

1 cup (c) = 8 fluid ounces (fl oz)  
 2 pints = 1 quart (qt)  
 2 cups = 1 pint (pt) = 16 fluid ounces  
 4 quarts = 1 gallon (gal)

### Weight

16 ounces (oz) = 1 pound (lb)  
 2000 pounds = 1 ton (T)

### Time

60 seconds (sec) = 1 minute (min)  
 60 minutes = 1 hour (hr)  
 24 hours = 1 day  
 7 days = 1 week

## Temperature

### Celsius (C) to Fahrenheit (F)

$$F = \frac{9}{5}C + 32$$

### Fahrenheit (F) to Celsius (C)

$$C = \frac{5(F - 32)}{9}$$

### Length

1 millimeter (mm) = 0.001 meter      1 m = 1000 mm  
 1 centimeter (cm) = 0.01 meter      1 m = 100 cm  
 1 decimeter (dm) = 0.1 meter      1 m = 10 dm  
 1 meter (m) = 1.0 meter  
 1 dekameter (dam) = 10 meters  
 1 hectometer (hm) = 100 meters  
 1 kilometer (km) = 1000 meters

### Capacity (Liquid Volume)

1 milliliter (mL) = 0.001 liter      1 L = 1000 mL  
 1 liter (L) = 1.0 liter  
 1 hectoliter (hL) = 100 liters  
 1 kiloliter (kL) = 1000 liters      1 kL = 10 hL

### Weight

1 milligram (mg) = 0.001 gram      1 g = 1000 mg  
 1 centigram (cg) = 0.01 gram  
 1 decigram (dg) = 0.1 gram  
 1 gram (g) = 1.0 gram  
 1 dekagram (dag) = 10 grams  
 1 hectogram (hg) = 100 grams  
 1 kilogram (kg) = 1000 grams      1 g = 0.001 kg  
 1 metric ton (t) = 1000 kilograms      1 kg = 0.001 t  
 1t = 1000 kg = 1,000,000 g = 1,000,000,000 mg

## US Customary and Metric Equivalents

### Length

1 in. = 2.54 cm (exact)      1 cm ≈ 0.394 in.  
 1 ft ≈ 0.305 m      1 m ≈ 3.28 ft  
 1 yd ≈ 0.914 m      1 m ≈ 1.09 yd  
 1 mi ≈ 1.61 km      1 km ≈ 0.62 mi

### Area

1 in.<sup>2</sup> ≈ 6.45 cm<sup>2</sup>      1 cm<sup>2</sup> ≈ 0.155 in.<sup>2</sup>  
 1 ft<sup>2</sup> ≈ 0.093 m<sup>2</sup>      1 m<sup>2</sup> ≈ 10.764 ft<sup>2</sup>  
 1 yd<sup>2</sup> ≈ 0.836 m<sup>2</sup>      1 m<sup>2</sup> ≈ 1.196 yd<sup>2</sup>  
 1 acre ≈ 0.405 ha      1 ha ≈ 2.47 acres

### Volume

1 in.<sup>3</sup> ≈ 16.387 cm<sup>3</sup>      1 cm<sup>3</sup> ≈ 0.06 in.<sup>3</sup>  
 1 ft<sup>3</sup> ≈ 0.028 m<sup>3</sup>      1 m<sup>3</sup> ≈ 35.315 ft<sup>3</sup>  
 1 qt ≈ 0.946 L      1 L ≈ 1.06 qt  
 1 gal ≈ 3.785 L      1 L ≈ 0.264 gal

### Mass

1 oz ≈ 28.35 g      1 g ≈ 0.035 oz  
 1 lb ≈ 0.454 kg      1 kg ≈ 2.205 lb

# Notation and Terminology

## Exponents

$$\underbrace{a \cdot a \cdot a \cdot \dots \cdot a}_n = a^n$$

← exponent  
← base

## Fractions

$$\frac{a}{b}$$

← numerator  
← denominator

## Least Common Multiple (LCM)

Given a set of whole numbers, the smallest number that is a multiple of each of these whole numbers.

## Ratios

$\frac{a}{b}$  or  $a:b$  or  $a$  to  $b$  A comparison of two quantities by division.

## Proportions

$\frac{a}{b} = \frac{c}{d}$  A statement that two ratios are equal.

## Greatest Common Factor (GCF)

Given a set of integers, the largest integer that is a factor (or divisor) of all of the integers.

## Types of Numbers

### Natural Numbers (Counting Numbers):

$$\mathbb{N} = \{1, 2, 3, 4, 5, 6, \dots\}$$

**Whole Numbers:**  $\mathbb{W} = \{0, 1, 2, 3, 4, 5, 6, \dots\}$

**Integers:**  $\mathbb{Z} = \{\dots, -4, -3, -2, -1, 0, 1, 2, 3, 4, \dots\}$

**Rational Numbers:** A number that can be written in the form  $\frac{a}{b}$  where  $a$  and  $b$  are integers and  $b \neq 0$ .

**Irrational Numbers:** A number that can be written as an infinite nonrepeating decimal.

**Real Numbers:** All rational and irrational numbers.

**Complex Numbers:** All real numbers and the even roots of negative numbers. The standard form of a complex number is  $a + bi$ , where  $a$  and  $b$  are real numbers,  $a$  is called the real part and  $b$  is called the imaginary part.

## Absolute Value

$|a|$  The distance a real number  $a$  is from 0.

## Equality and Inequality Symbols

- = “is equal to”
- ≠ “is not equal to”
- < “is less than”
- > “is greater than”
- ≤ “is less than or equal to”
- ≥ “is greater than or equal to”

## Sets



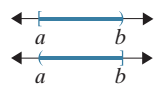


The **empty set** or **null set** (symbolized  $\emptyset$  or  $\{ \}$ ): A set with no elements.

The **union** of two (or more) sets (symbolized  $\cup$ ): The set of all elements that belong to either one set or the other set or to both sets.

The **intersection** of two (or more) sets (symbolized  $\cap$ ): The set of all elements that belong to both sets.

The word **or** is used to indicate union and the word **and** is used to indicate intersection.

## Algebraic and Interval Notation for Intervals

Type of Interval	Algebraic Notation	Interval Notation	Graph
Open Interval	$a < x < b$	$(a, b)$	
Closed Interval	$a \leq x \leq b$	$[a, b]$	
Half-open Interval	$\begin{cases} a \leq x < b \\ a < x \leq b \end{cases}$	$\begin{cases} [a, b) \\ (a, b] \end{cases}$	
Open Interval	$\begin{cases} x > a \\ x < b \end{cases}$	$\begin{cases} (a, \infty) \\ (-\infty, b) \end{cases}$	
Half-open Interval	$\begin{cases} x \geq a \\ x \leq b \end{cases}$	$\begin{cases} [a, \infty) \\ (-\infty, b] \end{cases}$	

## Radicals

The symbol  $\sqrt{\quad}$  is called a **radical sign**.

The number under the radical sign is called the **radicand**.

The complete expression, such as  $\sqrt{64}$ , is called a **radical** or **radical expression**.

In a cube root expression  $\sqrt[3]{a}$ , the number 3 is called the index. In a square root expression such as  $\sqrt{a}$ , the index is understood to be 2 and is not written.

## The Imaginary Number $i$

$$i = \sqrt{-1} \text{ and } i^2 = (\sqrt{-1})^2 = -1$$

# Formulas and Theorems

## Percent

$$\frac{P}{100} = \frac{A}{B} \quad (\text{the percent proportion}),$$

where

$$P\% = \text{percent (written as the ratio } \frac{P}{100} \text{)}$$

$B$  = base (number we are finding the percent of)

$A$  = amount (a part of the base)

$$R \cdot B = A \quad (\text{the basic percent equation}),$$

where

$R$  = **rate** or percent (as a decimal or fraction)

$B$  = **base** (number we are finding the percent of)

$A$  = **amount** (a part of the base)

## Profit

**Profit:** The difference between selling price and cost.

$$\text{profit} = \text{selling price} - \text{cost}$$

### Percent of Profit:

1. Percent of profit **based on cost:**  $\frac{\text{profit}}{\text{cost}}$
2. Percent of profit **based on selling price:**  $\frac{\text{profit}}{\text{selling price}}$

## Interest

**Simple Interest:**  $I = P \cdot r \cdot t$

**Compound Interest:**  $A = P \left( 1 + \frac{r}{n} \right)^n$

**Continuously Compounded Interest:**  $A = Pe^{rt}$

where

$I$  = interest (earned or paid)

$A$  = amount accumulated

$P$  = principal (the amount invested or borrowed)

$r$  = annual interest rate in decimal or fraction form

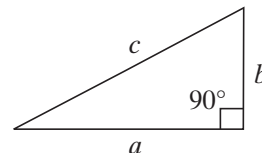
$t$  = time (one year or fraction of a year)

$n$  = the number of times per year interest is compounded

$e = 2.718281828459 \dots$

## The Pythagorean Theorem

In a right triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the two legs:  $c^2 = a^2 + b^2$



## Probability of an Event

probability of an event

$$= \frac{\text{number of outcomes in event}}{\text{number of outcomes in sample space}}$$

## Distance-Rate-Time

$d = rt$  The **distance traveled**  $d$  equals the product of the rate of speed  $r$  and the time  $t$ .

## Special Products

1.  $x^2 - a^2 = (x + a)(x - a)$ : Difference of two squares
2.  $x^2 + 2ax + a^2 = (x + a)^2$ : Square of a binomial sum
3.  $x^2 - 2ax + a^2 = (x - a)^2$ : Square of a binomial difference
4.  $x^3 + a^3 = (x + a)(x^2 - ax + a^2)$ : Sum of two cubes
5.  $x^3 - a^3 = (x - a)(x^2 + ax + a^2)$ : Difference of two cubes

## Change-of-Base Formula for Logarithms

For  $a, b, x, > 0$  and  $a, b \neq 1$ ,  $\log_b x = \frac{\log_a x}{\log_a b}$ .

## Distance Between Two Points

The distance  $d$  between points  $P(x_1, y_1)$  and  $Q(x_2, y_2)$  is  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ .

## Midpoint Formula

The midpoint between points  $P(x_1, y_1)$  and  $Q(x_2, y_2)$  is  $\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$ .

# Principles and Properties

## Properties of Addition and Multiplication

Property	Addition	Multiplication
<b>Commutative Property</b>	$a + b = b + a$	$ab = ba$
<b>Associative Property</b>	$(a + b) + c = a + (b + c)$	$a(bc) = (ab)c$
<b>Identity</b>	$a + 0 = 0 + a = a$	$a \cdot 1 = 1 \cdot a = a$
<b>Inverse</b>	$a + (-a) = 0$	$a \cdot \frac{1}{a} = 1 \ (a \neq 0)$

**Zero Factor Law:**  $a \cdot 0 = 0 \cdot a = 0$

**Distributive Property:**  $a(b + c) = a \cdot b + a \cdot c$

## Addition (or Subtraction) Principle of Equality

$A = B$ ,  $A + C = B + C$ , and  $A - C = B - C$  have the same solutions (where  $A$ ,  $B$ , and  $C$  are algebraic expressions).

## Multiplication (or Division) Principle of Equality

$A = B$ ,  $AC = BC$ , and  $\frac{A}{C} = \frac{B}{C}$  have the same solutions

(where  $A$  and  $B$  are algebraic expressions and  $C$  is any nonzero constant,  $C \neq 0$ ).

## Properties of Exponents

For nonzero real numbers  $a$  and  $b$  and integers  $m$  and  $n$ :

<b>The exponent 1</b>	$a = a^1$
<b>The exponent 0</b>	$a^0 = 1$
<b>The product rule</b>	$a^m \cdot a^n = a^{m+n}$
<b>The quotient rule</b>	$\frac{a^m}{a^n} = a^{m-n}$
<b>Negative exponents</b>	$a^{-n} = \frac{1}{a^n}$
<b>Power rule</b>	$(a^m)^n = a^{mn}$
<b>Power of a product</b>	$(ab)^n = a^n b^n$
<b>Power of a quotient</b>	$\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$

## Zero Factor Property

If  $a$  and  $b$  are real numbers, and  $a \cdot b = 0$ , then  $a = 0$  or  $b = 0$  or both.

## Properties of Rational Numbers (or Fractions)

If  $\frac{P}{Q}$  is a rational expression and  $P$ ,  $Q$ ,  $R$ , and  $K$  are polynomials where  $Q, R, S \neq 0$ , then

**The Fundamental Principle**  $\frac{P}{Q} = \frac{P \cdot K}{Q \cdot K}$

**Multiplication**  $\frac{P}{Q} \cdot \frac{R}{S} = \frac{P \cdot R}{Q \cdot S}$

**Division**  $\frac{P}{Q} \div \frac{R}{S} = \frac{P}{Q} \cdot \frac{S}{R}$

**Addition**  $\frac{P}{Q} + \frac{R}{Q} = \frac{P + R}{Q}$

**Subtraction**  $\frac{P}{Q} - \frac{R}{Q} = \frac{P - R}{Q}$

## Properties of Radicals

If  $a$  and  $b$  are positive real numbers,  $n$  is a positive integer,  $m$  is any integer, and  $\sqrt[n]{a}$  is a real number then

- $\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b}$
- $\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$
- $\sqrt[n]{a} = a^{\frac{1}{n}}$
- $a^{\frac{m}{n}} = \left(a^{\frac{1}{n}}\right)^m = (a^m)^{\frac{1}{n}}$   
or, in radical notation,  
 $a^{\frac{m}{n}} = (\sqrt[n]{a})^m = \sqrt[n]{a^m}$

## Properties of Logarithms

For  $b > 0$ ,  $b \neq 1$ ,  $x, y > 0$ , and any real number  $r$ ,

- $\log_b 1 = 0$
- $\log_b b = 1$
- $x = b^{\log_b x}$
- $\log_b b^x = x$
- $\log_b xy = \log_b x + \log_b y$  **The product rule**
- $\log_b \frac{x}{y} = \log_b x - \log_b y$  **The quotient rule**
- $\log_b x^r = r \cdot \log_b x$

## Properties of Equations with Exponents and Logarithms

For  $b > 0$ ,  $b \neq 1$ ,

- If  $b^x = b^y$ , then  $x = y$ .
- If  $x = y$ , then  $b^x = b^y$ .
- If  $\log_b x = \log_b y$ , then  $x = y$  ( $x > 0$  and  $y > 0$ ).
- If  $x = y$ , then  $\log_b x = \log_b y$  ( $x > 0$  and  $y > 0$ ).

# Equations and Inequalities

## Linear Equation in $x$ (First-Degree Equation in $x$ )

$ax + b = c$ , where  $a$ ,  $b$ , and  $c$  are real numbers and  $a \neq 0$ .

## Types of Equations and their Solutions

**Conditional:** Finite Number of Solutions

**Identity:** Infinite Number of Solutions

**Contradiction:** No Solution

## Linear Inequalities

**Linear Inequalities** have the following forms where  $a$ ,  $b$ , and  $c$  are real numbers and  $a \neq 0$ :

$$ax + b < c \quad \text{and} \quad ax + b \leq c$$

$$ax + b > c \quad \text{and} \quad ax + b \geq c$$

## Compound Inequalities

The inequalities  $c < ax + b < d$  and  $c \leq ax + b \leq d$  are called **compound linear inequalities**.

(This includes  $c < ax + b \leq d$  and  $c \leq ax + b < d$  as well.)

## Absolute Value Equations

For statements 1 and 2,  $c > 0$ :

1. If  $|x| = c$ , then  $x = c$  or  $x = -c$ .
2. If  $|ax + b| = c$ , then  $ax + b = c$  or  $ax + b = -c$ .
3. If  $|a| = |b|$ , then either  $a = b$  or  $a = -b$ .
4. If  $|ax + b| = |cx + d|$ , then either  $ax + b = cx + d$  or  $ax + b = -(cx + d)$ .

## Absolute Value Inequalities

For  $c > 0$ :

1. If  $|x| < c$ , then  $-c < x < c$ .
2. If  $|ax + b| < c$ , then  $-c < ax + b < c$ .
3. If  $|x| > c$ , then  $x < -c$  **or**  $x > c$ .
4. If  $|ax + b| > c$ , then  $ax + b < -c$  **or**  $ax + b > c$ .

(These statements hold true for  $\leq$  and  $\geq$  as well.)

## Quadratic Equation

An equation that can be written in the form  $ax^2 + bx + c = 0$ , where  $a$ ,  $b$ , and  $c$  are real numbers and  $a \neq 0$ .

## Quadratic Formula

The solutions of the general quadratic equation  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ .

## The Discriminant

The expression  $b^2 - 4ac$ , the part of the quadratic formula that lies under the radical sign, is called the **discriminant**.

If  $b^2 - 4ac > 0$ , there are two real solutions.

If  $b^2 - 4ac = 0$ , there is one real solution,  $x = -\frac{b}{2a}$ .

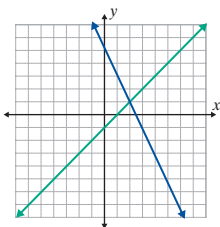
If  $b^2 - 4ac < 0$ , there are two nonreal solutions.

# Systems of Linear Equations

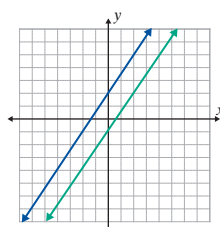
## Systems of Linear Equations (Two Variables)

The system is...

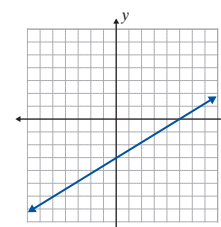
**consistent**, and  
the equations are **independent**.  
(One solution)



**inconsistent**, and  
the equations are **independent**.  
(No solution)



**consistent**, and  
the equations are **dependent**.  
(Infinite number of solutions)



# Functions

## Function, Relation, Domain, and Range

A **relation** is a set of ordered pairs of real numbers.

The **domain**  $D$  of a relation is the set of all first coordinates in the relation.

The **range**  $R$  of a relation is the set of all second coordinates in the relation.

A **function** is a relation in which each domain element has exactly one corresponding range element.

## One-to-One Functions

A function is a **one-to-one function** if for each value of  $y$  in the range there is only one corresponding value of  $x$  in the domain.

## Algebraic Operations with Functions

- $(f + g)(x) = f(x) + g(x)$
- $(f - g)(x) = f(x) - g(x)$
- $(f \cdot g)(x) = f(x) \cdot g(x)$
- $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}$
- $(f \circ g)(x) = f(g(x))$

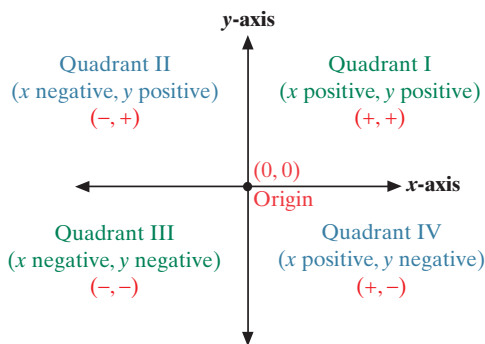
## Inverse Functions

If  $f$  is a one-to-one function with ordered pairs of the form  $(x, y)$ , then its **inverse function**, denoted as  $f^{-1}$ , is also a one-to-one function with ordered pairs of the form  $(y, x)$ .

If  $f$  and  $g$  are one-to-one functions and  $f(g(x)) = x$  for all  $x$  in  $D_g$  and  $g(f(x)) = x$  for all  $x$  in  $D_f$ , then  $f$  and  $g$  are **inverse functions**.

# Graphs of Functions

## The Cartesian Coordinate System



## Linear Functions (Lines)

**Standard form:**

$$Ax + By = C \quad \text{Where } A \text{ and } B \text{ do not both equal } 0$$

**Slope of a line:**

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{Where } x_1 \neq x_2$$

**Slope-intercept form:**

$$y = mx + b \quad \text{With slope } m \text{ and } y\text{-intercept } (0, b)$$

**Point-slope form:**

$$y - y_1 = m(x - x_1) \quad \text{With slope } m \text{ and point } (x_1, y_1) \text{ on the line}$$

**Horizontal line, slope 0:**  $y = b$

**Vertical line, undefined slope:**  $x = a$

**Parallel lines** have the same slope.

**Perpendicular lines** have slopes that are negative reciprocals of each other.

## Quadratic Functions (Parabolas)

**Parabolas of the form**  $y = ax^2 + bx + c$ :

1. Vertex:  $\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$ .

2. Line of Symmetry:  $x = -\frac{b}{2a}$

**Parabolas of the form**

$$y = a(x - h)^2 + k:$$

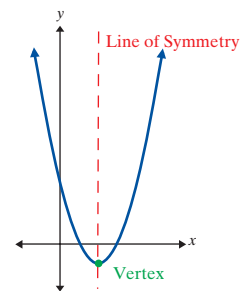
1. Vertex:  $(h, k)$

2. Line of Symmetry:  $x = h$

3. The graph is a horizontal shift of  $h$  units and a vertical shift of  $k$  units of the graph of  $y = ax^2$ .

**In both cases:**

- If  $a > 0$ , the parabola "opens upward."
- If  $a < 0$ , the parabola "opens downward."



# Conic Sections

## Equations of a Horizontal Parabola

$x = ay^2 + by + c$  or  $x = a(y - k)^2 + h$  where  $a \neq 0$ .

The parabola opens left if  $a < 0$  and right if  $a > 0$ .

The vertex is at  $(h, k)$ .

The line  $y = k$  is the line of symmetry.

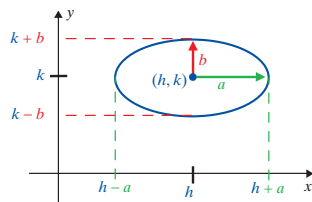
## Equation of an Ellipse

The standard form for the equation of an ellipse with its

center at the origin is  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .

The points  $(a, 0)$  and  $(-a, 0)$  are the  $x$ -intercepts (called vertices).

The points  $(0, b)$  and  $(0, -b)$  are the  $y$ -intercepts (called vertices).



When  $a^2 > b^2$ :

- The segment of length  $2a$  joining the  $x$ -intercepts is called the major axis.
- The segment of length  $2b$  joining the  $y$ -intercepts is called the minor axis.

When  $b^2 > a^2$ :

- The segment of length  $2b$  joining the  $y$ -intercepts is called the major axis.
- The segment of length  $2a$  joining the  $x$ -intercepts is called the minor axis.

The standard form for the equation of an ellipse with its

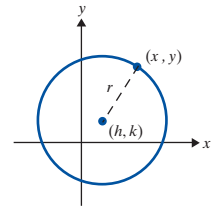
center at  $(h, k)$  is  $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$ .

## Equation of a Circle

The equation of a circle with

radius  $r$  and center  $(h, k)$  is

$$(x-h)^2 + (y-k)^2 = r^2.$$



## Equation of a Hyperbola

In general, there are two standard forms for equations of hyperbolas with their centers at the origin.

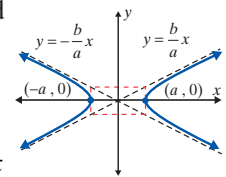
$$1. \quad \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

$x$ -intercepts (vertices) at  $(a, 0)$  and  $(-a, 0)$

No  $y$ -intercepts

Asymptotes:  $y = \frac{b}{a}x$  and  $y = -\frac{b}{a}x$

The curves "open" left and right.



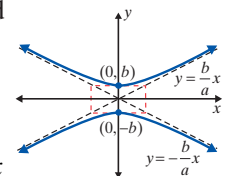
$$2. \quad \frac{y^2}{b^2} - \frac{x^2}{a^2} = 1$$

$y$ -intercepts (vertices) at  $(0, b)$  and  $(0, -b)$

No  $x$ -intercepts

Asymptotes:  $y = \frac{b}{a}x$  and  $y = -\frac{b}{a}x$

The curves "open" up and down.



The equation of a hyperbola with its center at  $(h, k)$  is

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1 \quad \text{or} \quad \frac{(y-k)^2}{b^2} - \frac{(x-h)^2}{a^2} = 1$$